Cold Damping of an Optically Levitated Nanoparticle to Microkelvin Temperatures

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(Received 24 December 2018; published 3 June 2019)

We implement a cold-damping scheme to cool one mode of the center-of-mass motion of an optically levitated nanoparticle in ultrahigh vacuum ($10^{-8}$ mbar) from room temperature to a record-low temperature of 100 μK. The measured temperature dependence on the feedback gain and thermal decoherence rate is in excellent agreement with a parameter-free model. For the first time, we determine the imprecision-backaction product for a levitated optomechanical system and discuss the resulting implications for ground-state cooling of an optically levitated nanoparticle.

DOI: 10.1103/PhysRevLett.122.223601

Introduction.—The interaction of light and matter is at the heart of a host of precision measurements, ranging from the detection of gravitational waves to the definition of the international unit system [1,2]. What makes electromagnetic fields our probe of choice is the availability of detectors and laser light sources that operate at the noise limit dictated by the laws of quantum mechanics. Shortly after the invention of the laser, the scientific community started to explore the possibilities of mechanical manipulation of matter using the forces of light in optical traps [3,4]. These forces can be interpreted as the inevitable consequence of the measurement process resulting from light-matter interaction [5]. Thus, optical forces and measurement precision are linked according to the Heisenberg uncertainty principle. The investigation of these measurement backaction effects has generated the field of optomechanics, which has developed experimental platforms that allow both measurement and control of mechanical motion at the quantum limit using light fields [6–10].

A different type of optomechanical system are dielectric particles levitated in optical traps [11–16]. These levitated systems complement traditional mechanically tethered structures in applications ranging from precision measurements [17–20] to the investigation and control of quantum states of massive objects [21]. For levitated and mechanically clamped oscillators alike, the investigation of unexplored physics, such as the experimental testing of collapse models [22], requires cooling the oscillator’s motion to its quantum ground state. This feat has been achieved for cryogenically precooled mechanically clamped systems using autonomous cavity cooling [23,24]. Despite the remarkable development of cavity-based cooling techniques [25–28], the most successful cooling method in levitated optomechanics to date has been parametric feedback cooling in a single-beam optical dipole trap [15,29]. This endeavor has led to mean occupation numbers of the center-of-mass motion below 100 phonons [30]. In contrast, in the realm of mechanically tethered oscillators and trapped ions, a different active feedback cooling method termed cold damping has been developed [31–35]. This measurement-based feedback technique applies a direct force to the oscillator in proportion to its speed, effectively leading to an increased damping rate [36]. Cold damping has recently been used to bring a cryogenically precooled, cavity-coupled membrane to its quantum ground state of motion [37]. Given the success of cold damping in the context of cooling mechanically tethered oscillators, it is a tantalizing prospect to adapt the technique to optically levitated nanoparticles in single-beam dipole traps. In particular, levitated optomechanics could greatly benefit from the theoretical insights available thanks to the thorough understanding of the dynamics of cold-damped oscillators. Surprisingly, the potential of cold damping for ground-state cooling the motion of an optically levitated nanoparticle has remained unexplored to date.

In this Letter, we cool the center-of-mass motion of an optically levitated nanoparticle along one axis to a temperature of 100 μK using cold damping. To this end, we exploit the Coulomb force acting on the net electric charge carried by the particle [38–40]. We investigate the cooling performance as a function of the gas pressure and feedback gain to explore the limitations of the method. Our system operates a factor of 1000 from the Heisenberg limit of the imprecision-backaction product and provides a platform for studying ground-state cooling of optically levitated oscillators.

Experimental.—Our experimental setup is shown in Fig. 1. We optically trap a silica nanoparticle (diameter 136 nm) in a linearly polarized laser beam (wavelength 1064 nm, focal power 130 mW), focused by a microscope.
frequency shifted by 1 MHz from the trapping light. We backscattered light, using a local oscillator which is such that the feedback signal is proportional to the biquad filters, which essentially mimics a derivative filter, function

\[ \frac{\partial^2}{\partial t^2} \]

of mass are resulting oscillation frequencies of the particle plane along (orthogonal to) the axis of polarization. We exert a Coulomb force on the net charge carried by the trapping potential irrelevant from the measurement signal for different feedback gains, which we express as damping rates \( \gamma_{FB} \). We extract the damping rate \( \gamma_{FB} \) from ring-down measurements as detailed further below. The measured signal \( S_{il}^\text{pol} \), corresponds to a Lorentzian function added to a spectrally flat noise floor due to the photon shot noise on our detector. The spectral width of the Lorentzian is a measure for the total damping rate arising from feedback cooling and residual gas damping. The latter is largely negligible under feedback at the low gas pressures of our experiments. The area under the Lorentzian, on the other hand, is a measure for the energy (i.e., temperature) of the particle’s oscillation mode. As expected, as we increase the feedback gain, the Lorentzian broadens in width and simultaneously shrinks in area. Thus, from the PSD of the out-of-loop signal \( S_{ol}^\text{pol} \), we extract the energy \( k_B T_y \), in the y mode of the levitated particle (with \( k_B \) the Boltzmann constant).

In Fig. 2(b), we plot the measured mode temperature \( T_y \) as a function of feedback damping rate \( \gamma_{FB} \) at a pressure of \( 1.4 \times 10^{-8} \) mbar as black circles. At small feedback gains, we observe a decrease in the oscillator temperature with an increasing feedback gain. However, there exists an optimal feedback gain of about 1 kHz. For gain values larger than the optimum, the oscillator temperature increases with an increasing feedback gain. For comparison, we show the PSD of the measured out-loop signal \( S_{ol}^\text{pol} \) at the same gain values as in Fig. 2(a). For a large feedback gain, we observe that \( S_{ol}^\text{pol} \) drops below the shot-noise level. This effect, termed noise squashing, arises from correlations between the particle’s position and the measurement noise that is fed back by the control loop [32,33]. In Fig. 2(b), we additionally show measurements performed at a higher pressure of \( 1.2 \times 10^{-7} \) mbar (gray triangles), where the increased gas damping rate leads to a larger mode temperature as compared to the low-pressure data.

Analysis.—To understand our results, let us analyze our system from a theoretical perspective [32]. The Fourier transform \( \tilde{y}(\Omega) \) of the time-dependent particle position \( y(t) \) follows the equation of motion

\[ \tilde{y}(\Omega) = \tilde{y}_{\text{heat}} \]

where \( \Omega \) is the \( \gamma \) mode’s eigenfrequency, \( m \) is the particle’s mass, and \( \tilde{y}_{\text{heat}} \) is the measurement shot noise on the in-loop

FIG. 1. Experimental setup. A silica nanoparticle (nominal diameter 136 nm) carrying a finite net charge \( q \) is optically trapped in a vacuum using a laser beam (wavelength 1064 nm) focused by an objective. To measure the \( y \) motion of the particle, the backscattered light is rerouted by a free-space circulator, mixed with a local oscillator (frequency shifted by 1 MHz relative to the trap laser), and sent to a balanced split detection scheme, yielding the out-of-loop signal \( y_{ol} \). The forward-scattered light is detected in another balanced split detection scheme and yields the in-loop signal \( y_{il} \), which is processed by a linear, digital filter \( H \). The resulting feedback signal is applied as a voltage to a capacitor enclosing the trapped particle.
detector, which measures \( \hat{y}_{d} = \hat{y} + \hat{S}_{v} \). The damping rate \( \gamma \) arises from the interaction with residual gas molecules. The term \( \hat{f}_{\text{fluct}} \) describes the fluctuating force generated by the interaction with the gas and from radiation pressure shot noise. Via the fluctuation dissipation theorem, \( \hat{f}_{\text{fluct}} \) is intrinsically linked to \( \gamma \) [44]. Within the bandwidth of interest, the transfer function of our feedback circuit is well described by \( H(\Omega) = -i \gamma_{FB} \Omega \). The feedback damping rate \( \gamma_{FB} \) can be set by adjusting the feedback gain and incorporates the exact geometry of the capacitor electrodes and the number of charges carried by the levitated particle. Importantly, the feedback transfer function \( H(\Omega) \) appears twice in Eq. (1), which results from the fact that the input to the feedback circuit \( \hat{y}_{d} \) is the sum of the true position \( \hat{y} \) and the measurement shot noise \( \hat{S}_{v} \). From Eq. (1), we obtain the two-sided PSD on the out-of-loop detector

\[
S_{y_{d}}^{ol}(\Omega) = \frac{S_{B}/m^{2} + \gamma_{FB}^{2} \frac{S_{nn}}{(\Omega^{2} - \Omega_{0}^{2})^{2}}}{(\Omega^{2} - \Omega_{0}^{2})^{2} + (\gamma + \gamma_{FB})^{2} \Omega^{2}} + S_{v_{w}},
\]

where \( S_{B} \) denotes the PSD of the fluctuating force \( \hat{f}_{\text{fluct}} \) and \( S_{nn} (S_{v_{w}}) \) are the PSDs of the in-loop (out-of-loop) detector noise. Integrating the first term of Eq. (2), which corresponds to the PSD of the true position \( \hat{y} \), in the limit \( \gamma_{FB} \gg \gamma \) yields the variance

\[
\langle \hat{y}^{2} \rangle = \frac{\pi S_{B}}{m^{2} \gamma_{FB} \Omega_{0}^{2}} + \pi \gamma_{FB} S_{nn},
\]

which is a direct measure for the temperature \( T_{y} = m \Omega_{0}^{2} \langle \hat{y}^{2} \rangle / k_{B} \) of the oscillator mode. The first term contributing to the expression in Eq. (3) scales with the inverse of the feedback cooling rate \( \gamma_{FB} \). This term resembles the desired action of the feedback, which is to reduce the impact of the heating term given by the fluctuating force \( S_{B} \). Importantly, the second term is proportional to the feedback damping rate, which multiplies with the measurement noise \( S_{nn} \). This term resembles the undesired but inevitable effect of the control loop heating the particle by feeding back measurement noise. Accordingly, our model predicts the existence of an optimum feedback cooling rate, where the mode temperature reaches its minimum value \( T_{\text{min}} = 2 \pi \Omega_{0} \sqrt{S_{B} S_{nn}} / k_{B} \), a behavior that we observe in our measurements in Fig. 2(b).

For a quantitative comparison of the measurements and theory, we have to determine all parameters entering Eq. (3). We extract the in-loop measurement noise \( S_{nn} \) from the PSD shown in the inset in Fig. 2(b). To obtain the feedback damping rate \( \gamma_{FB} \), we perform ring-down measurements. To this end, we toggle the feedback gain back and forth between \( \gamma_{FB} \) for 30 \( \mu \)s and a much lower feedback gain \( \gamma_{FB}^{\text{low}} = \gamma_{FB} / 300 \) for 50 \( \mu \)s. As shown in Fig. 3, we measure the mode temperature as a function of the time after the gain was switched from \( \gamma_{FB}^{\text{low}} \) to \( \gamma_{FB} \) at time \( t = 0 \). The blue triangles in Fig. 3(a) are the ensemble average over 100 such decay curves. We observe an exponential decay of the temperature and extract its time constant, which equals \( \gamma_{FB} \). Next, we determine the heating rate...
Equipped with the experimentally determined values for the bath and measurement noise (red) to Eq. (3). Our model describes our experimental findings very well. We stress that there is no free parameter or fit involved.

Finally, we investigate the reheating speed and the ring-down rate γ_{FB} as a function of the pressure. The results are displayed in Fig. 3(b). We find that the ring-down rates (blue triangles) do not depend on the pressure. This observation confirms that the damping rate under feedback is indeed fully dominated by and therefore equivalent to the cold-damping rate γ_{FB}. The red circles in Fig. 3(b) show the measured reheating speeds dT_{y}/dt as a function of the pressure, which follow the expected linear behavior (dash-dotted line).

Discussion.—Let us discuss the current limitations and future prospects of our cold-damping approach for levitated optomechanics. To this end, we return to Eq. (3), whose two contributions are related by the imprecision-backaction product S_{FB}S_{nn} = \frac{1}{2}(\hbar/4\pi)^2, with the measurement efficiency η ≤ 1 [44]. At the optimal feedback gain, we find an effective phonon occupation number n = k_{B}T/(\hbar\Omega) 1/2 that depends solely on η as n_{min} = \frac{1}{2}[(1/\sqrt{\eta}) - 1] [37]. At the Heisenberg limit of unit efficiency η = 1, when the fluctuating force S_{FB} driving the system under investigation is purely due to measurement backaction, and the imprecision noise S_{nn} is minimized by optimally detecting all photons scattered by the levitated particle, the particle’s motion could, in principle, be brought to its quantum ground state n_{min} = 0. In our case, at the lowest investigated pressure of 1.4 × 10^{-8} mbar, we extract a total efficiency of η = 9 × 10^{-4} and, hence, an occupation number of about 16. Our measurements in Fig. 3(b) suggest that we can further reduce S_{FB} by moving to even lower pressures, before entering the regime where reheating is fully dominated by photon recoil [30]. The factor S_{nn} in our case is limited by the finite collection and detection efficiency. The latter is restricted by the nonideal mode overlap between the scattered dipole field and the Gaussian trapping beam on the detector. Exploiting the Purcell-enhanced collection and detection efficiency of a cavity, a suppression of S_{nn} by more than one order of magnitude seems realistic [25,27,28]. Accordingly, occupation numbers approaching unity appear within reach.

Conclusion.—In conclusion, we have demonstrated cold damping of the center-of-mass motion of an optically levitated nanoparticle from room temperature to 100 μK, corresponding to less than 20 phonons. We have determined the optimal feedback-damping rate for our system, in excellent agreement with a parameter-free model. Together with photonic techniques under development [28,45], our results put ground-state cooling of optically levitated nanoparticles firmly within reach. Besides setting a new temperature benchmark, we believe that our feedback control scheme will serve as a model system for the levitated optomechanics community. Putting our work into context, our approach is complementary to parametric

Given by S_{FB}. When the feedback gain is switched from γ_{FB} to γ_{FB \text{low}} at time t = 0, we observe the mode temperature increasing linearly in time [red circles in Fig. 3(a)], averaged over 100 reheating experiments. Since the observed time is much shorter than the inverse damping rate γ_{B}, we expect the temperature to increase as T(t) = γ_{FB}T_{bath}t. Together with the fluctuation dissipation theorem S_{FB} = m\gamma k_{B}T_{bath}/\pi, the measured slope of the reheating curve therefore provides us with a direct measurement of the first term in Eq. (3) [44]. Equipped with the experimentally determined values for γ_{FB}, S_{nn}, and S_{FB}, we calculate the mode temperature as a function of the feedback gain according to Eq. (3) and display it as the solid black line in Fig. 2(b). The dashed lines show the two separate contributions from the bath (blue) and measurement noise (red) to Eq. (3). Our model describes our experimental findings very well. We stress that there is no free parameter or fit involved.
feedback cooling, the method of choice to control charge-neutral optically levitated particles. In contrast, our system relies on the levitated object carrying a finite net charge. Importantly, our work provides the direct connection between established, mechanically tethered optomechanical technologies and optically levitated oscillators [32,33,37]. By mapping our optically levitated system onto the standard model of a cold-damped oscillator, for the first time, we have determined the imprecision-backaction product for a levitated optomechanical system. Accordingly, our work generates the opportunity to leverage the insights gained with mechanically clamped systems to drive levitated optomechanics forward.

This research was supported by ERC-QMES (Grant No. 338763) and the NCCR-QSIT program (Grant No. 51NF40-160591). We thank R. Diehl, E. Hebestreit, van der Laan, R. Reimann, and D. Windey for valuable input and discussions.

Note added in proof.—We have recently become aware of related work by Conangla et al. [46].

We define our PSDs according to 
\[
\begin{align*}
\langle y^2 \rangle &= \int_0^{\infty} df \tilde{S}_{yy}(f) = \\
&= \int_{-\infty}^{\infty} d\Omega S_{yy}(\Omega).
\end{align*}
\]